Design of humanitarian supply chain system by applying the general two-stage network DEA model

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Abstract

Purpose – The recent COVID-19 outbreak and severe natural disasters make the design of the humanitarian supply chain network (HSCN) a crucial strategic issue in a pre-disaster scenario. The HSCN design problem deals with the location/allocation of emergency response facilities (ERFs). This paper aims to propose and demonstrate how to design an efficient HSCN configuration under the risk of ERF disruptions.

Design/methodology/approach – This paper considers four performance measures simultaneously for the HSCN design by formulating a weighted goal programming (WGP) model. Solving the WGP model with different weight values assigned to each performance measure generates various HSCN configurations. This paper transforms a single-stage network into a general two-stage network, treating each HSCN configuration as a decision-making unit with two inputs and two outputs. Then a two-stage network data envelopment analysis (DEA) approach is applied to evaluate the HSCN schemes for consistently identifying the most efficient network configurations.

Findings – Among various network configurations generated by the WGP, the single-stage DEA model does not consistently identify the top-ranked HSCN schemes. In contrast, the proposed transformation approach identifies efficient HSCN configurations more consistently than the single-stage DEA model. A case study demonstrates that the proposed transformation method could provide a more robust and consistent evaluation for designing efficient HSCN systems. The proposed approach can be an essential tool for federal and local disaster response officials to plan a strategic design of HSCN.

Originality/value – This study presents how to transform a single-stage process into a two-stage network process to apply the general two-stage network DEA model for evaluating various HSCN configurations. The proposed transformation procedure could be extended for designing some supply chain systems with conflicting performance metrics more effectively and efficiently.

Keywords Humanitarian supply chain network, Weighted goal programming, General two-stage network process, Data envelopment analysis, Emergency response facility

Paper type Research paper

1. Introduction

The humanitarian supply chain network (HSCN) plays a critical role in providing disaster relief items such as medicine, drinking water, food and daily commodities to alleviate people's suffering. The year 2017 became a historic year of weather and climate disasters for the United States, which, in total, was impacted by 16 separate billion-dollar disaster events, including three tropical cyclones, two inland floods, eight severe storms, a crop freeze, drought and wildfire. In early 2019, Alaska, the coldest state in the US, posted its warmest March on record by a landslide and the powerhouse storm in the central US became the second billion-dollar weather disaster of 2019. The year 2020 set the new annual record of 22 events, breaking the previous record of 16 events in 2011 and 2017. During 2020 and 2021, the US experienced a very active year of weather and climate disasters (see Figure 1), including the COVID-19 pandemic. According to the data developed by the NOAA's National Climatic Data Center, the US, on average, faces ten severe weather events yearly exceeding one billion dollars in damage (see Figure 2). A comparison with an annual average of only two such events throughout the 1980s clearly may force us to speculate that a warming climate could make these disasters more frequent and intense. In this respect, an HSCN design has become an important strategic decision due to the significant damage inflicted by several natural disasters (Petrudi *et al.*, 2020). Moreover, COVID-19 and its variants have brought issues of emergency relief planning through the HSCN again.

The HSCN is defined as the flow of relief aid and related information between people from disaster-stricken areas and donors to alleviate the suffering of vulnerable people. Indeed, after emergencies, it is critical for emergency response facilities (ERFs) to distribute humanitarian aid to the affected areas

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Figure 1 US billion-dollar weather and climate disasters (2021)

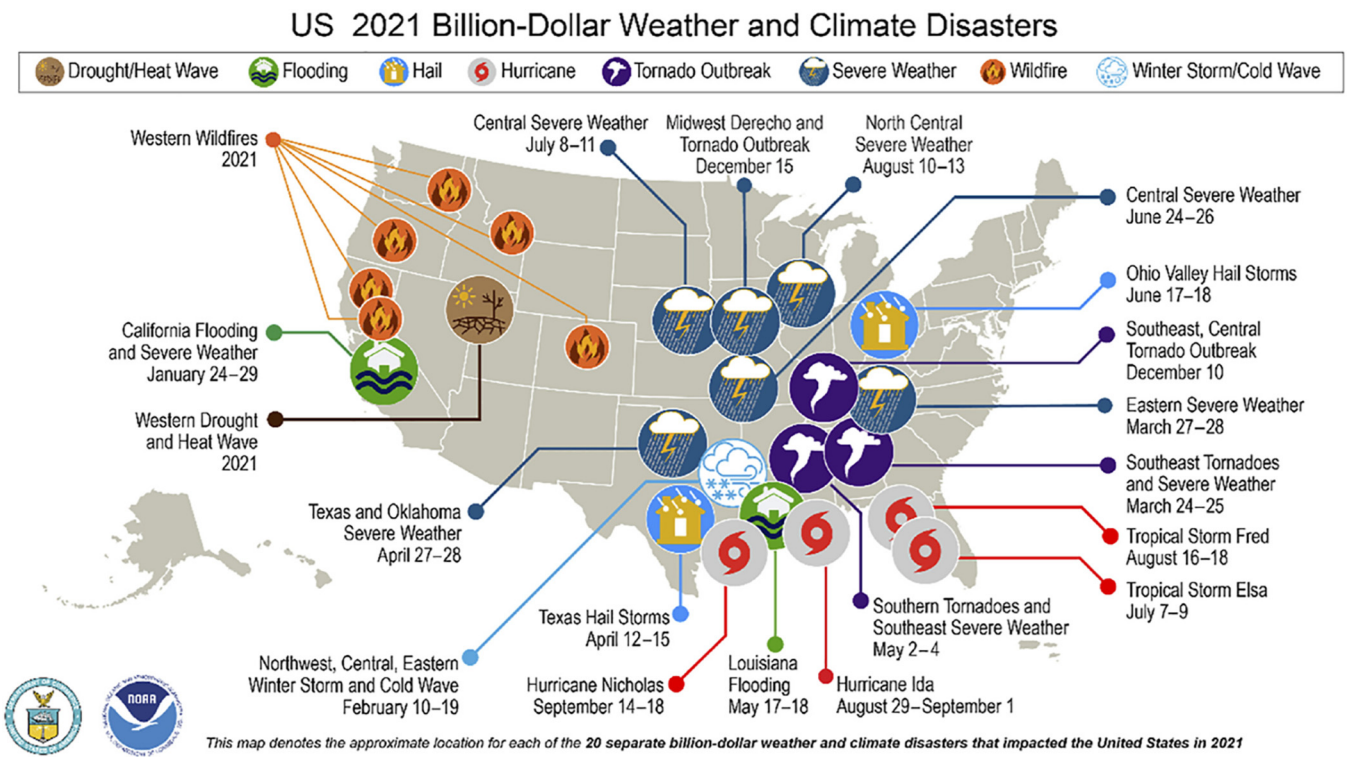
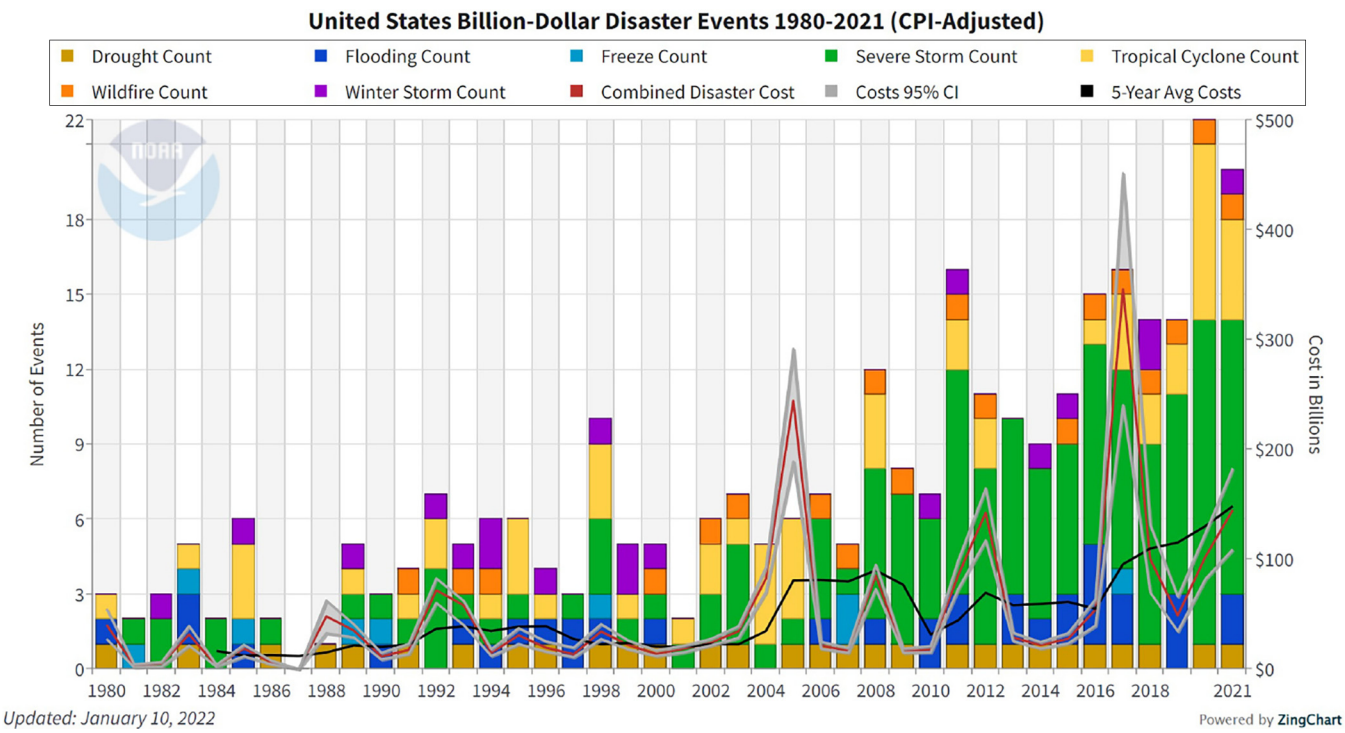


Figure 2 Billion-dollar disasters by type, from 1980 to 2021



efficiently and effectively to save human lives and alleviate suffering and rapid recovery. Van Wassenhove (2006) emphasizes that since disaster relief is 80% logistics, it would follow that the only way to operate the HSCN system efficiently and effectively is through efficient, effective and slick logistics operations, and more precisely, supply chain management. Logistics planning in emergencies involves the quick and efficient distribution of emergency supplies from the ERFs to

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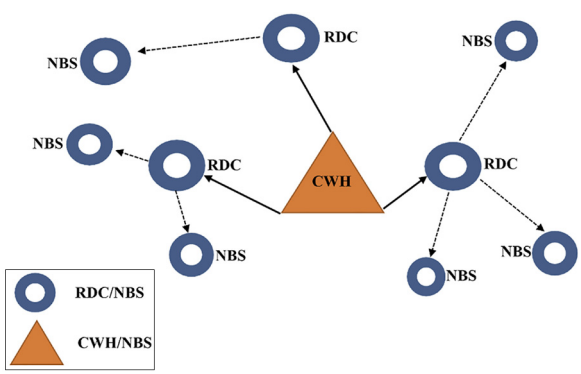
the affected areas via supply chains. Several authors (Boonmee *et al.*, 2017; Cao *et al.*, 2018; Hong and Jeong, 2019; Petrudi *et al.*, 2020; Sarma *et al.*, 2020) have considered various HSCN design models. Zhang *et al.* (2019) and Liu *et al.* (2019) have reviewed the papers on the HSCN design problems. Gress *et al.* (2021) present a methodology for designing an HSCN to distribute COVID-19 vaccines in Mexico. Malmir and Zobel (2021) propose a sustainable HSCN design model considering the COVID-19 outbreak.

The ERFs considered in this paper are three distinctive ones. They are (1) central warehouses (CWHs) or distribution warehouses, where emergency relief commodities are stored, (2) intermediate response facilities termed relief distribution centers (RDCs) or commodity distribution points and (3) neighborhood sites (NBSs), which are affected areas in need of humanitarian items. These ERFs are depicted in Figure 3 by modifying Habib *et al.* (2016).

As mentioned above, an HSCN design problem is inherently strategic and long-term. The main objective of the strategic level is to strengthen emergency preparedness as well as to select the most cost/distance-effective location of CWHs and RDCs among a set of candidate locations, to establish the distribution of emergency supplies throughout the HSCN and to assign NBSs to RDCs and RDCs to CWHs. Making such a decision is a critical area in designing an effective HSCN. However, traditional cost-based facility location-allocation models implicitly assume that located facilities will always be in service or available and do not consider an associated risk of disruption. But all facilities are susceptible to natural/weather disasters, strikes, or pandemics. A lack of flexibility and interdependency in the HSCN could aggravate the effects of disruptions. Snyder *et al.* (2016) review nearly 150 articles related to the OR/MS literature on supply chain disruptions to take stock of the research and provide an overview of the research questions. They predict that the literature on supply disruptions will continue to increase over the coming years, identifying seven topics as avenues for future research. Li *et al.* (2020) investigate supply chain network characteristics that can better understand supply chain resilience under disruption risk propagation. Aldrighetti *et al.* (2021) review more than 220 articles on the quantitative models of supply chain network design under disruption risks in industrial supply chain management and logistics, highlighting drawbacks and missing aspects in the related literature and discussing future research

Figure 3 Distribution framework of humanitarian supply chain



directions. Ganesh and Kalpana (2022) point out that though the research on supply chain risk management (SCRM) remains for an extended period; industries still face difficulties managing supply chain risks. Also, supply chain managers have begun to focus on decision-making based on numerous data sources for predicting uncertainties more accurately to achieve a proactive and predictive intelligent risk management mechanism. These characteristics make artificial intelligence (AI) and machine learning (ML) suitable SCRM techniques. Emphasizing that these AI techniques are in an emerging stage in SCRM, they (2022) provide unexploded and missing aspects in current research, challenge on implementing AI technologies and describe promising avenues for the future after reviewing 127 papers on SCRM.

The typical multi-objective programming model allows the decision-maker to decide weights for the objective function's deviational variables. It mainly reflects the importance and desirability of deviations from the various goals. However, the actual efficiency of the resulting HSCN is not known. Ragsdale (2018) states that there is no standard procedure for assigning values to the weight factors to guarantee finding the most desirable solution. He suggests that it will be necessary for the decision-makers to follow an iterative procedure. Decision-makers could try a particular set of weights, solve the problem, analyze the solution and then refine the weights and solve it again. He concludes that it is essential for the decision-makers to repeat this process several times to find the most desirable solution. Thus, it is unavoidable for decision-makers to use some of their subjective judgment.

Then, a challenging question is how the best alternative option can be selected if the most desirable solution is different among the decision-makers. It would be imperative to evaluate the efficiency of all alternatives generated by the model and select the most desirable one(s) with an optimized objective function or without any subjective judgment. Following this vein, Hong and Jeong (2019) apply a single-stage network data envelopment analysis (SSN-DEA) method for evaluating the various HSCN schemes generated by solving the multi-objective programming models formulated for the HSCN design problem.

For the SSN process, the conventional DEA (C-DEA) method proposed by Charnes *et al.* (1978) has been widely accepted as an effective performance evaluation tool for assessing the relative efficiency of a set of peer entities called decision-making units (DMUs). C-DEA determines which DMUs make efficient use of their inputs and produce most outputs and which do not. Thus, the C-DEA model classifies DMUs into two groups, i.e. separating efficient DMUs from inefficient DMUs, using efficiency score (ES). The analysis indicates where an inefficient DMU might look for benchmarking help to search for ways to improve. Each DMU is evaluated with its most favorable weights due to the DEA's nature of self-evaluation, ignoring unfavorable inputs or outputs to raise self-efficiency. As a result, C-DEA's critical weakness of a lack of discrimination is caused because it classifies a considerable number of DMUs out of the set of DMUs as efficient, with an ES equal to 1.

Sexton *et al.* (1986) propose a cross-evaluation concept to do the peer evaluation rather than the C-DEA's pure self-evaluation to remedy this deficiency. Doyle and Green (1994) suggest a cross-evaluation matrix for ranking the units by applying the cross-efficiency DEA (CE-DEA) model. Generally, the CE

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evaluation can provide a full ranking for the DMUs. But, as Doyle and Green (1994) find, the non-uniqueness of cross-efficiency scores (CESs) and non-consistent rankings have been critical issues for applying the CE-DEA. Another concept for peer evaluation is the super-efficiency DEA (SE-DEA), which is introduced to compensate for the weaknesses of C-DEA and CE-DEA. A DMU under evaluation is excluded from the DEA models' reference set. The resulting model is called a SE-DEA model that has significance for discriminating among efficient DMUs. Charnes *et al.* (1992) use the SE model to study the efficiency classification's sensitivity. Anderson and Peterson (1993) propose the SE model to rank the efficient DMUs. But the critical issue of using the model is that the adjacent DMUs decide the super efficiency score (SEC) of an efficient DMU, so it would be awkward for DMUs to be ranked by the SESs.

As big data research becomes an essential area of operations analytics, DEA has evolved into a tool for big data analysis. As Cook and Zhu (2014) mention, an important development area in the DEA applications has been devoted to applications wherein DMUs represent network processes. In fact, a network DEA has been significant steam that controls efficiencies of various sub-stages in a complex structure. A substantial body of DEA research has focused on the network DEA since the network DEA can satisfy three defining properties of big data, volume, variety and velocity (Zhu, 2022). DMUs may consist of two or more stage network structures with intermediate measures. Monfared and Safi (2013) state that the SSN-DEA model considers a DMU as a "black box" and neglects intervening processes, i.e. different series or parallel functions. Thus, the "black box" approaches for the single-stage process provide no insights regarding the inter-relationships among the components' inefficiencies and cannot offer specific process guidance to DMU managers to improve DMU's efficiency.

Out of the literature on the optimization models for HSCN, Hong and Jeong (2019) consider four performance measures simultaneously using the multi-objective programming (MOP) model. Then, they apply the SSN-DEA method to find the efficient configurations out of the various HSCN configurations generated by the MOP model. Their work (2019) would be the first attempt to combine the MOP model with the SSN-DEA method in the literature on the design of HSCN. Monfared and Safi (2013), Cook and Zhu (2014) and Zhu (2022) state the strengths of the TSN-DEA in contrast to the weaknesses of the SSN-DEA.

Many authors have considered the single-stage HSCN design problem using multi-objective programming models. Single-stage network DEA (SSN-DEA) models have recently been applied to evaluate the efficiency of designed HSCN schemes. As mentioned, the SSN-DEA methods show several intrinsic weaknesses, such as ignoring the intervening processes and producing inconsistent rankings. The SSN-DEA model's most critical weakness lies in its inconsistent efficiency score (ES), which depends on the DMUs under evaluation in the reference sets. For example, the top-ranked DMU based on the ESs when all DMUs are evaluated should maintain the top-ranking position even though some lower-ranked DMUs are not assessed together. But the SSN- DEA models frequently allow the previously lower-ranked DMU to overtake the top-ranked DMU to become a new #1 DMU if some lower-ranking DMUs are not evaluated together. Thus, the research questions on the SSN-DEA's weaknesses have been raised by various authors.

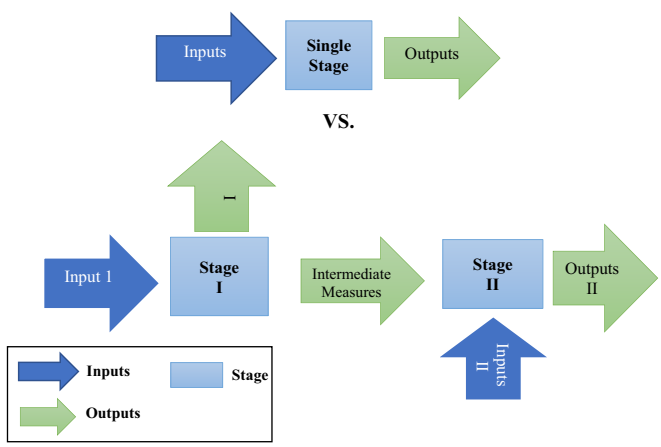
There is a research gap in evaluating DMUs with a single-stage network process since, as mentioned above, SSN-DEA methods do not consider the intervening processes. Moreover, these SSN-DEA methods do not rank the efficient DMUs consistently. Thus, the research question is how to transform the single-stage HSCN system into a general two-stage network (GTSN) process system so that GTSN-DEA (GTSN-DEA) model is applied to compensate for the weaknesses of the SSN-DEA models for the HSCN design problem. To answer these questions, this paper proposes transforming a single-stage HSCN design problem into a two-stage network (TSN) process to apply the GTSN-DEA model. See Figure 4, depicting the SSN-GTSN-DEA structures. We identify efficient HSCN configurations among the schemes generated by solving the WGP model for various weight set values for the transformed TSN process. Using the case study, we demonstrate that the proposed approach shows a better analysis of the efficiency of the designed HSCN configurations and produces more consistent and robust rankings after evaluating efficient HSCN configurations. Thus, the contribution of this paper is to reveal the could-be hidden network schemes, if SSN-DEA is only applied, that the decision-makers would not consider as the candidate schemes for their final decision.

The proposed two-stage network design problem differs from the two-stage stochastic programming model with the high uncertainty in the decision environment, such as uncertainty of inputs and outputs at each stage. The paper considers a decision environment with no uncertainty, such as given inputs and outputs. After GTSN-DEA is applied, an additional research question is how to investigate whether the GTSN-DEA ranks the top-rated DMUs more consistently. In fact, this study would be the first attempt to answer these kinds of research questions for the HSCN design problem in a pre-disaster scenario, which consists of finding the optimal ERFs under the risk of facility disruption.

2. Formulation of humanitarian supply chain design problem

The following nomenclature is used throughout the paper to formulate a multi-objective mathematical model (see Hong and Jeong, 2019):

Figure 4 Single-stage vs. general two-stage network DEA structure



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Sets

I	index set of candidate locations for CWHs (i =1, 2, ..., ω)
N	index set of NBSs n (n =1, 2, ..., η)
G	G ={N, I}, index set of NBSs and CWHs (g =1, 2, ..η, $\eta+1$, ..., $\eta+\omega$)
J	index set of candidate locations for RDCs (j =1, 2, η, $\eta+1$, ..., $\eta+\omega$)

Parameters

f_i	fixed cost for constructing and operating CWH_i
b_j	fixed cost for constructing and operating RDC_j
a^1_{ij}	shipping cost per mile per one unit of demand from CWH_i to RDC_j
a^2_{jm}	shipping cost per mile per one unit of demand from RDC_j to NBS_m
d_{ij}	distance between CWH_i and RDC_j
d_{jg}	distance between RDC_j and NBS_g
C^{max}	maximum number of RDCs can be built
CAP_i^{max}	capacity of CWH_i
CAP_j^{max}	capacity of RDC_j
H_g	demand of NBS_g (can be either NBS or RDC or CWH)
W^{max}	maximum number of CWHs can be built
k_i	minimum number of RDCs that CWH_i can handle
K_i	maximum number of RDCs that CWH_i can handle
l_j	minimum number of NBSs that RDC_j can cover
L_j	maximum number of NBSs that RDC_j can cover

Decision variables

C_j	binary variable deciding whether neighborhood *j* is selected as RDC_j
W_i	binary variable deciding whether a candidate CWH_i is selected
w_{ij}	binary variable deciding whether RDC_j is covered by CWH_i
r_{jg}	binary variable deciding whether location g is covered by RDC_j
z_{ijg}	binary variable deciding whether location g is covered by CWH_i through RDC_j

Assumption

(i) When an ERF, RDC, or CWH is damaged or disrupted by natural or environmental occurrences, it can't cover any demand that it is supposed to cover
(ii) RDCs can be located at any NBSs and potential CWH locations, while a CWH can be built in one of the potential CWH locations only since CWH locations must satisfy some realistic location requirements
(iii) An RDC must cover any unselected CWH locations and must not be located at the selected CWH location
(iv) An RDC covers the demands of the NBSs it covers, including its demand
(v) A CWH covers its demand and demands from its covered RDCs

The first goal is minimizing the related logistics costs, which is the traditional objective of most FLA models. Given this problem set, the total logistics cost (TLC) consists of the expenses for CWHs (construction, operation and distribution of items from CWHs to RDCs) and the costs for RDCs (building and development as well as distribution of relief items from RDCs to NBSs):

$$TLC = \left[\sum_{i\in I} f_i W_i + \sum_{i\in I}\sum_{j\in G}\left(\sum_{g\in G} H_g\right) a^1_{ij} d_{ij} w_{ij} r_{jg} + \sum_{j\in G} b_j C_j + \sum_{j\in G}\sum_{g\in G} H_g a^2_{jg} d_{jg} r_{jg}\right]. \quad (1)$$

The next goal is related to the demand-oriented objective, which focuses on measuring the "closeness" of the ERFs. In other words, ERFs should be located at a place close to the covered sites to deliver the relief item as quickly as possible. The second goal is to minimize the maximum coverage distance (MCD) such that each NBS is covered by one of the RDCs, and each RDC is covered by one of the CWHs within the endogenously determined distance. This goal minimizes the longest delivery distance between CWHs and RDCs, and RDCs and NBSs. As the MCD increases, it will cause ineffectiveness to the resulting HSCN. Now, MCD is given by

$$MCD = Max\{d_{jg} r_{jg,}\ d_{ij} w_{ij}\},\ \forall i, j,\ and\, g. \quad (2)$$

The ERFs should be located at the least likely locations to be disrupted to enhance supply chain resilience to inevitable disasters. The third goal related to the least likely locations to be disrupted is to maximize the expected amount of covered demands (ECD) by the ERFs, which is expressed as

$$ECD = \sum_{i\in I}\sum_{j\in G}\left[\sum_{g\in G}(1-q_i)(1-p_j)(z_{ijg} H_g)\right] + \sum_{i\in I}(1-q_i)(H_i W_i), \quad (3)$$

where

p_j = the probability that the RDC_j is disrupted (or risk probability);

q_i = the probability that the CWH_i is disrupted (or risk probability).

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In case of emergency, each resident should be within a certain distance of the nearest centers to be served. Also, some environmental difficulties or constraints, such as weather issues and road damage, may limit the maximum coverage distance of MCD in (2). Thus, the maximum effective coverage distance in case of emergency, denoted by D_c, would be shorter than MCD. In addition, it is desirable to maximize the covered demands within D_c, while minimizing MCD. The next goal is to maximize the covered demands in case of emergency, CDE, which is expressed as

$$CDE = \sum_{g\in G}\sum_{j\in \mathcal{J}} H_g \kappa_{jg} r_{jg} + \sum_{i\in I} H_i W_i \tag{4}$$

where an indicator parameter, κ_{jg}, is

$$\kappa_{jg} = \begin{cases} 1, \ if\ d_{jg} \le D_c \\ 0, \ otherwise. \end{cases} \tag{5}$$

Let the nonnegative deviation variables, δ^+_{TLC}, δ^+_{MCD}, δ^-_{ECD}, and δ^-_{CDE}, represent the amounts by which each value of TLC, MCD, ECD and CDE deviates from the target values. Using $\alpha = \{\alpha_1, \alpha_2, \alpha_3, \alpha_4\}$ and $\sum_{\kappa=1}^{4} \alpha_\kappa = 1$ denote relative weights attached to the corresponding goal, the following weighted goal programming (WGP) model can be formulated:

$$Min\, Z_\alpha = \alpha_1 \frac{\delta^+_{TLC}}{TLC_{min}} + \alpha_2 \frac{\delta^+_{MCD}}{MCD_{min}} + \alpha_3 \frac{\delta^-_{ECD}}{ECD_{max}} + \alpha_4 \frac{\delta^-_{CDE}}{CDE_{max}}, \tag{6}$$

subject to

$$TLC\, in\, (1) - \delta^+_{TLC} = TLC_{min}, \tag{7}$$

$$MCD\, in\, (2) - \delta^+_{MCD} = MCD_{min}, \tag{8}$$

$$ECD\, in\, (3) + \delta^-_{ECD} = ECD_{max}, \tag{9}$$

$$CDE\, in\, (4) + \delta^-_{CDE} = CDE_{max}. \tag{10}$$

$$\sum_{i\in I} W_i \le W^{max}, \tag{11}$$

$$W_i + C_{\eta+i} \le 1, \ \forall i \in I \tag{12}$$

$$W_i + \sum_{j\in M} r_{j(\eta+i)} = 1, \ \forall i \in I \tag{13}$$

$$\sum_{j\in G} r_{jn} = 1, \ \forall n \in N \tag{14}$$

$$W_i\, k_i \le \sum_{j\in G} w_{ij} \le W_i K_i, \ \forall i \in I \tag{15}$$

$$\sum_{i\in I} w_{ij} = C_j, \ \forall j \in G \tag{16}$$

$$\sum_{j\in G} C_j \le C^{max}, \tag{17}$$

$$r_{jg} \le C_j, \ \forall j\ and\ \forall g \in G \tag{18}$$

$$C_j \cdot l_j \le \sum_{g\in G} r_{jg} \le C_j \cdot L_j, \ \forall j \in G \tag{19}$$

$$\sum_{g\in G} H_g r_{jg} \le CAP_j^{max}, \ \forall j \in G \tag{20}$$

$$\sum_{j\in G}\sum_{g\in G} H_g z_{ijg} + H_i W_i \le CAP_i^{max}, \ \forall i \in I \tag{21}$$

Constraints (11) define the upper bound of the number of CWHs that can be built. Here at most W^{max} is allowed. Constraints (12) ensure that the potential CWH location will not be selected simultaneously as both CWH and RDC. Constraints (13) ensure that if a potential CWH location i is not selected (*i.e.*, $W_i = 0$), its demand must be satisfied by an RDC or a CWH. Constraints (14) make certain that each NBS ($n \in N$) is assigned to either an RDC or a CWH. Constraints (15) limit the minimum and maximum number of RDCs to be covered by each CWH. Constraints (16) ensure that CWHs only supply the selected RDCs. Constraints (17) limit the total number of selected RDCs to be less than or equal to a user-specified number, C^{max}. Constraints (18) ensure that NBSs or unselected CWH locations can only be assigned to the selected candidate RDCs. Constraints (19) ensure that the chosen candidate RDC$_j$ must cover a minimum number of l_j NBSs and can only cover a maximum of L_j NBSs. Constraints (20) and (21) show the shipping capacity of RDCs and CWHs, respectively. Solving the above WGP model in (6)–(21) for a given set of weights would generate an HSCN network scheme. Thus, by changing the weight set, various HSCNs could be developed. Each network scenario could be treated as a DMU for the DEA method to be applied to evaluate all scenarios with two inputs, TLC and MCD and two outputs, ECD and CDE.

As shown in Eq. (6), the objective function of WGP is to minimize the weighted sum of the percentage deviations. The above WGP model is an extension of the GP model, whose objective is to minimize the sum of the deviations. The above weighted GP model differs from the epsilon (ε) multi-objective optimation method, where one objective will be used as the objective function, and the remaining objectives will be used as constraints using the epsilon. Lexicographic GP is another version of GP when a specific goal is strictly preferable to the other goals, or the decision maker has a clear preference order for achieving the goals.

3. Single-stage vs. general two-stage network model

First, as shown in Figure 5, the SSN model is applied. DMUs, equivalent to the HSCN schemes generated by solving the WGP model for different weight values assigned to each goal, can be evaluated by applying the DEA method. The mathematical model of the SSN-DEA model for DMU$_\omega$, is given by

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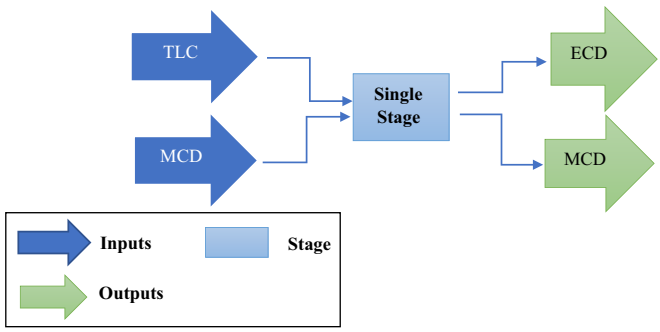
Figure 5 Single-stage network (SSN) DEA structure for HSCN system



$$max\theta_\omega = [u_1 ECD_\omega + u_2 CDE_\omega], \tag{22}$$

subject to

$$v_1 TLC_\omega + v_2 MCD_\omega = 1. \tag{23}$$

$$(u_1 ECD_\kappa + u_2 CDE_\kappa) - [v_1 TLC_\kappa + v_2 MCD_\kappa] \leq 0, \forall \kappa \tag{24}$$

$$u_r,\ v_i \geq 0,\ r = 1,\ 2;\ i = 1,\ 2,$$

where u_r is a weight or coefficient assigned by DEA to output r, and v_i is the weight or coefficient assigned by DEA to input i. Let θ^*_ω, efficiency score (ES), represent the optimal value of the objective function in (22) corresponding to the optimal solution (u^*, v^*). DMU_ω is said to be efficient with θ^*_ω of 1.

The CE-DEA method consists of two phases. The first phase is self-evaluation, where DEA scores are calculated using the model by (22)–(24). In the second phase, the weights arising from the first phase are applied to all DMUs to get the cross-efficiency score (CES) for each DMU. Let $E_{\omega\omega}$ represent the DEA score for DMU_ω and $u^*_{r\omega}$ and $v^*_{i\omega}$ denote the optimal solution obtained from solving (22)–(24). Now, the cross efficiency of DMU_j using a rating DMU_ω is

$$E_{\omega j} = \frac{u^*_{1\omega} ECD_j + u^*_{2\omega} CDE_j}{[v^*_{1\omega} TLC2_j + v^*_{2\omega} MCD_j]},\ \omega \neq j. \tag{25}$$

By averaging $E_{j\omega}$ in (25), the CES of DMU_ω is given by

$$\overline{E}_\omega = \frac{1}{\Omega}\sum_{j=1}^{\Omega} E_{j\omega}. \tag{26}$$

A super-efficiency DEA (SE-DEA) would generate a super-efficiency score (SES) obtained from the C-DEA model after a DMU under evaluation is excluded from the reference set. Thus, the SESs of efficient DMUs can have higher values than 1, the maximum value of the ES obtained by other DEA methods. The SE-DEA model is given by

$$max\theta_\omega = [u_1 ECD_\omega + u_2 CDE_\omega], \tag{27}$$

subject to

$$v_1 TLC_\omega + v_2 MCD_\omega = 1, \tag{28}$$

$$(u_1 ECD_\kappa + u_2 CDE_\kappa) - [v_1 TLC_\kappa + v_2 MCD_\kappa] \leq 0, \forall \kappa \neq \omega,$$

$$u_r,\ v_i \geq 0,\ r = 1,\ 2;\ i = 1,\ 2. \tag{29}$$

The SSN model can be decomposed into an equivalent GTSN model, as shown in Figure 6. In other words, an HSCN network scheme is decomposed into two stages, i.e. stage 1 represents the flows from CWHs to RDCs, while stage 2 represents the flows of items from RDCs to NBSs. The two inputs, TLC and MCD, are split into TLC1 and MCD1 for stage 1 and TLC2 and MCD2 for stage 2, respectively. An output ECD is divided into ECD0 and ECD1 for stage 1 and ECD2 for stage 2. The ECD0 denote the ECD for the sites where CWHs are located, while ECD1 becomes an intermediate measure that flows from stage 1 to stage 2. Now, the split inputs and outputs are expressed as

$$TLC1 = \left[\sum_{i\in I} f_i W_i + \sum_{i\in I}\sum_{j\in G}\left(\sum_{g\in G} H_g\right) a^1_{ij} d_{ij} w_{ij}\right], \tag{30}$$

$$TLC2 = \left[\sum_{j\in G} b_j C_j + \sum_{j\in G}\sum_{g\in G} H_g a^2_{jg} d_{jg} r_{jg}\right], \tag{31}$$

$$MCD1 = Max\{\, d_{ij} w_{ij}\},\ \forall i\ and\ j, \tag{32}$$

$$MCD2 = Max\{d_{jg} r_{jg}\},\ \forall j\ and\ g, \tag{33}$$

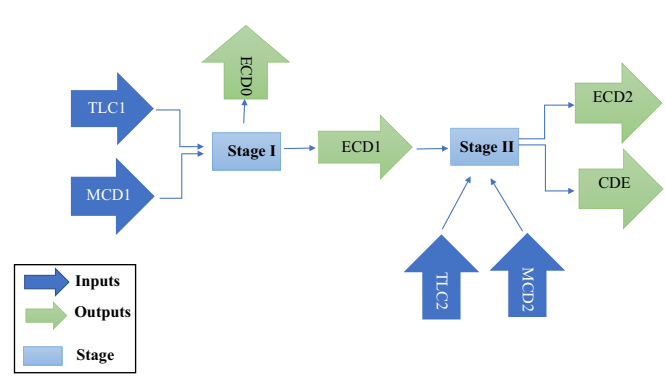
$$ECD0 = \sum_{i\in I}(1 - q_i)(W_i H_i), \tag{34}$$

$$ECD1 = \sum_{i\in I}\sum_{j\in G}(1 - q_i)(w_{ij} H_j), \tag{35}$$

$$ECD2 = ECD - ECD0$$
$$= \sum_{i\in I}\sum_{j\in G}\left[\sum_{g\in G}(1 - q_i)(1 - p_j)(z_{ijg} H_g)\right], \tag{36}$$

where the expression of ECD is given in (4). Since each stage in Figure 4 works together to achieve the best performance of the

Figure 6 General two-stage network (GTSN) DEA structure for HSCN system



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HSCN, a centralized model is applied to analyze the converted two-stage network.

$$\theta_\omega^1 = \frac{\lambda_1 ECD0_\omega + \eta_1 ECD1_\omega}{v_1 TLC1_\omega + v_2 MCD1_\omega}, \tag{37}$$

$$\theta_\omega^2 = \frac{u_1 ECD2_\omega + u_2 CDE_\omega}{\eta_1 ECD1_\omega + [Q_1 TLC2_\omega + Q_2 MCD2_\omega]}. \tag{38}$$

where θ_ω^1 and θ_ω^2 are ESs of stages 1 and 2 for DMU$_\omega$, respectively, and the weights for each input, output and intermediate one are $\{v_1, v_2, Q_1, Q_2, \lambda_1, u_1, u_2, \eta_1\} \geq 0$. Now, the overall centralized ES, θ_ω^{cen}, can be given by:

$$\theta_\omega^{cen} = Max\{\theta_\omega^1 in\,(37) * \theta_\omega^2 in\,(38)\}, \tag{39}$$

subject to

$$\frac{\lambda_1 ECD0_\kappa + \eta_1 ECD1_\kappa}{v_1 TLC1_\kappa + v_2 MCD1_\kappa} \leq 1, \forall \kappa \tag{40}$$

$$\frac{u_1 ECD2_\kappa + u_2 CDE_\kappa}{\eta_1 ECD1_\kappa + [Q_1 TLC2_\kappa + Q_2 MCD2_\kappa]} \leq 1, \forall \kappa \tag{41}$$

Let θ_ω^{1max} be the maximum efficiency score of stage 1, then the following LP model for the model in (39)–(41) is formulated:

$$\theta_\omega^{1max} = max\{\lambda_1 ECD0_\omega + \eta_1 ECD1_\omega\}, \tag{42}$$

subject to

$$v_1 TLC1_\omega + v_2 MCD1_\omega = 1. \tag{43}$$

$$\lambda_1 ECD0_\kappa + \eta_1 ECD1_\kappa - (v_1 TLC1_\kappa + v_2 MCD1_\kappa) \leq 0, \forall \kappa \tag{44}$$

$$(u_1 ECD2_\kappa + u_2 CDE_\kappa) - w_1 ECD1_\kappa - [Q_1 TLC2_\kappa + Q_2 MCD2_\kappa] \leq 0, \forall \kappa \tag{45}$$

$$v_1, v_2, \lambda_1, \eta_1, u_1, u_2, w_1, Q_1, Q_2 \geq 0$$

From (42)–(45), the optimal value of (42), an estimator θ_ω^1 for the first stage, is a variable whose maximum value is θ_ω^{1max}. Now, the overall (centralized) ES for the two-stage model, θ_ω^{cen*}, is a function of θ_ω^1 and can be formulated as:

$$\theta_\omega^{cen*} = max\{\theta_\omega^1 * [u_1 ECD2_\omega + u_2 CDE_\omega]\}, \tag{46}$$

subject to

$$\lambda_1 ECD0_\kappa + \eta_1 ECD1_\kappa - (v_1 TLC1_\kappa + v_2 MCD1_\kappa) \leq 0, \forall \kappa \tag{47}$$

$$(u_1 ECD2_\kappa + u_2 CDE_\kappa) - \eta_1 ECD1_\kappa - [Q_1 TLC2_\kappa + Q_2 MCD2_\kappa] \leq 0, \forall \kappa \tag{48}$$

$$Q_1 TLC2_\omega + Q_2 MCD2_\omega + w_1 ECD1_\omega = 1, \tag{49}$$

$$\lambda_1 ECD0_\omega + \eta_1 ECD1_\omega - \theta_\omega^1 (v_1 TLC1_\omega + v_2 MCD1_\omega) = 0, \tag{50}$$

$$\theta_\omega^1 \leq \theta_\omega^{1max}. \tag{51}$$

$$v_1, v_2, \lambda_1, \eta_1, u_1, u_2, w_1, Q_1, Q_2 \geq 0$$

Li *et al.* (2012) propose an iteration method by setting $\theta_\omega^1 = \theta_\omega^{1max} - z\Delta\varepsilon$, where $\Delta\varepsilon$ is a step size and $z = 0, 1, 2, \ldots, z^{max} + 1$, $z^{max} \leq \left[\frac{\theta_\omega^{1max}}{\Delta\varepsilon}\right]$.. The optimal global efficiency of the system under evaluation is estimated as $\theta_\omega^{cen*} = max\, z\theta_\omega^{cen,1}(z)$. Now the formal procedure can be stated as follows:

Procedure

1 Step 1: *[Identifying efficient DMUs for SSN-DEA Model]*
   - Using the m-DEA method, evaluate all DMUs by solving an LP given in (22)–(24).
   - Identifying efficient DMUs where their ESs are equal to 1, $\theta_\omega = 1$ and stratify them into a set G^1.
   - Using (25)–(26) and (27)–(29), obtain the CESs and SESs for the DMUs in Θ^1 and rank them based on these two ESs.

2 Step 2: *[Decomposing and Applying GTSN-DEA Model]*
   - For DMUs in Θ^1, decompose the SSN model into a GTSN model.
   - Setting $\theta_\omega^1 = \theta_\omega^{1max} - z\Delta\varepsilon$, $z = 0, 1, 2, \ldots, z^{max} + 1$, $z^{max} \leq \left[\frac{\theta_\omega^{1max}}{\Delta\varepsilon}\right]$, set $\theta_\omega^{cen*} = max\, z\theta_\omega^{cen,1}(z)$.
   - Rank the DMUs in G^1 based on θ_ω^{cen*} in (v).

4. Case study and observations

A case study uses major disaster declaration records in South Carolina (SC). We cluster forty-six (46) counties based on proximity and populations into twenty (20) counties. Then, one location from each clustered county based on a centroid approach is chosen by assuming that all population within the grouped county exists in that location. Federal Emergency Management Agency (FEMA) database shows that SC has experienced sixteen (16) major natural disaster declarations, such as tornadoes, hurricanes, floods, etc., from 1964 to 2017. The database also lists counties where a major disaster was declared. This paper assumes that the county's emergency facility is disrupted and shut down when a major disaster is declared. Based on the historical record and the assumption, each neighborhood's risk probability (a county or a clustered county) is calculated in Table 1 by dividing the years with major natural disasters by the total years. The five potential locations for CWHs are selected based upon population, the proportion of area that each site would potentially cover and the proximity to Interstate Highways in SC.

The number of RDCs and CWHs to be built are pre-specified in most cases. We simplify the TLC function given by Eq. (1) by excluding the fixed cost terms for RDCs and CWHs. If the actual data are available for the fixed cost terms, we can readily lift such restrictions to obtain more revealing results.

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Table 1 Data for locations of ERFs

No	City	County	Population (K)	Risk probability
1	Anderson	Anderson/Oconee/Pickens	373	0.125
2	Beaufort	Beaufort/Jasper	187	0.063
3	Bennettsville	Marlboro/Darlington/Chesterfield	96	0.375
4	Conway	Horry	269	0.375
5	Georgetown	Georgetown/Williamsburg	93	0.438
6	Greenwood	Greenwood/Abbeville	92	0.125
7	Hampton	Hampton/Allendale	33	0.188
8	Lexington	Lexington/Newberry/Saluda	318	0.313
9	McCormick	McCormick/Edgefield	35	0.250
10	Moncks Corner	Berkeley	178	0.313
11	Orangeburg	Orangeburg/Bamberg/Calhoun	123	0.375
12	Rock Hill	York/Chester/Lancaster	321	0.313
13	Spartanburg	Spartanburg/Cherokee/Union	367	0.313
14	Sumter	Sumter/Clarendon/Lee	157	0.375
15	Walterboro	Colleton/Dorchester	135	0.250
16	*Aiken†*	*Aiken/Barnwell*	*184*	*0.313*
17	*Charleston†*	*Charleston*	*350*	*0.250*
18	*Columbia†*	*Richland/Fairfield/Kershaw*	*461*	*0.375*
19	*Florence†*	*Florence/Dillon/Marion*	*203*	*0.438*
20	*Greenville†*	*Greenville/Laurens*	*521*	*0.125*

Note: †Potential locations for CWH

Also, the following parameters are pre-determined for our case study. The maximum numbers of RDCs and CWHs that can be built, C^{max} and W^{max}, are set to 5 and 2, respectively. The minimum and maximum number of RDCs that a CWH must handle, k_i and K_i, are set to 1 and 10, respectively. Each RDC must handle at least 2 ($\ell_j = 2$) and at most 7 ($L_j = 7$) NBSs. The capacities of RDCs and CWHs, CAP_j^{max} and CAP_i^{max}, $\forall j$ *and* $\forall i$, are set to 1,500 K and 2,500 K in terms of the number of humanitarian items.

The WGP model is solved for various values of weight, $\boldsymbol{\alpha} = \{\alpha_1, \alpha_2, \alpha_3, \alpha_4\}$. Each weight alters between 0 and 1 with an increment of 0.1, subject to $\sum_{\kappa=1}^{4} \alpha_\kappa = 1$. We use the 'Gurobi' Solver Engine of Analytic Solver software. Two hundred eighty-six (286) configurations arising out of the combinations of the setting of $\boldsymbol{\alpha}$ are solved on an Intel® Xeon ® Gold 5122 HP Z4 Workstation PC (2 processors) with 32 GB of RAM installed using a 64-bit version of Windows 10. It takes 10,238 s (approximately 2.84 h) to solve all 286 sets of the GP model. On average, it takes 35.8 s to solve one weight set of the GP. The 286 configurations are reduced to sixty-eight (68) consolidated structures since several cases yield the same values of the four-performance metrics. Each of the 68 configurations is considered a DMU, representing the optimal locations and allocations of ERFs.

As Step 1 in the procedure proposes, we apply the C-DEA model in (22)–(24) for the SSN, as shown in Figure 5, to find efficient DMUs with a perfect ES of 1.000. Twenty-six (26) DMUs with ES equal to 1.000 identified from the 68 consolidated DMUs are reported in Table 2, as the ES in the last column indicates. Using Eqs (30)–(36), we decompose the inputs and outputs of those 26 efficient DMUs (see Figure 6) and also list them in Table 2, starting with TLC1 from the 3rd column. Now, we apply CE- and SE-DEA of the SSN-DEA to compute the cross-efficiency score (CES) and super-efficiency score (SES) for each efficient DMU. We also apply the GTSN-DEA in Step 2 using the decomposed inputs and outputs listed in Table 2. These efficiency scores for the SSN- and GTSN-DEA are reported in Table 3 where θ_ω^1 and θ_ω^2 denote ESs of stages 1 and 2, respectively, and the overall centralized ES, θ_ω^{cen}, are reported along with the corresponding rank, [R], based on each efficiency score. Table 3 shows that each approach finds a different DMU as the top-ranked one. DMU_{133} and DMU_{87} are ranked #1 by CES and SES, respectively, for the SSN-DEA model. The GTSN-DEA ranks DMU_{174} as #1, based on the overall efficiency, θ_ω^{cen*}. We observe that DMU_{133}, ranked #1 by CES, is surprisingly ranked #4 and #17 by SES and θ_ω^{cen*}. We also note that DMU_{87}, ranked #1 by SES, is ranked #17 and #26 by the other two methods. The GTSN's #1 ranked DMU_{174} is ranked #24 and #3 by CES and SES.

Table 2 compares these three top-ranked DMUs and shows each DMU has dominating inputs or outputs. For example, DMU_{87} with a perfect ES, i.e. $\theta_{87}^2 = 1$, at stage 2, as shown in Table 3, has the smallest two inputs to stage 2, TLC2 and MCD2, and the greatest output from stage 2, CDE, whereas DMU_{174}, with a perfect ES, $\theta_{174}^1 = 1$ at stage 1, has the smallest two inputs to stage 1, TLC1 and MCD1, and the greatest outputs, ECD0, ECD1 and ECD2, but the lowest CDE among these three top DMUs. Inputs and outputs for DMU_{133} ranked #1 by CES, are listed between the other two top-ranked DMUs, DMU_{87} and DMU_{174}.

To investigate the robustness of ranks generated by each method, we select eighteen (18) DMUs out of twenty-six (26) efficient DMUs shown in Tables 2 and 3 These 18 DMUs ranked at least #9 by any efficiency score are evaluated and reported in Table 4. For comparison purposes, besides the new ranking, [R], based on the current efficiency score, the expected ranking, E[R], based on the rankings in Table 3, where 26 DMUs are ranked, is also reported in Table 4. For

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Table 2 Efficient DMUs, their performance metrics and efficiency scores

No	DMU #	TLC1 Input (1,1)	MCD1 Input (1, 2)	ECD0 (K) Output (1,1)	ECD1 (K) Output (1,2)	TLC2 Input (2, 1)	MCD2 Input (2, 2)	ECD2 (K) Output (2,1)	CDE (K) Output (2,2)	ES
1	25	$268,201	93.5	570	2,628	$125,179	97.3	1,913	3,092	1.000*
2	26	$269,775	93.5	570	2,628	$123,530	97.3	1,913	3,092	1.000*
3	28	$194,148	92.5	718	2,960	$177,303	92	2,357	2,038	1.000*
4	34	$271,081	93.5	570	2,628	$129,763	97.3	1,913	3,092	1.000*
5	35	$266,975	92.5	570	2,628	$131,582	92	1,950	2,852	1.000*
6	38	$221,122	92.5	718	2,962	$191,948	92	2,390	1717	1.000*
7	39	$313,022	97.3	240	2,550	$113,550	87	1,868	3,178	1.000*
8	40	$319,446	97.3	240	2,597	$125,339	95.7	1,951	3,178	1.000*
9	42	$218,580	85.6	744	2,619	$144,874	82.2	1,979	2,185	1.000*
10	43	$187,169	85.6	744	2,619	$158,082	82.2	2,011	2,139	1.000*
11	81	$229,285	104	718	2,965	$102,438	82.9	2,093	2,827	1.000*
12	87	$279,656	104	402	2,280	$105,574	92	1,697	3,361	1.000*
13	88	$259,611	92.5	570	2,628	$121,145	97.3	1,881	3,092	1.000*
14	89	$204,337	98.6	744	2,614	$138,925	97.3	1,903	2,889	1.000*
15	91	$169,518	92.5	718	2,942	$172,186	92	2,291	2,038	1.000*
16	97	$174,738	85.6	744	2,619	$155,965	80.7	1,976	2,139	1.000*
17	98	$179,818	85.6	744	2,619	$155,251	80.7	1,990	2,139	1.000*
18	101	$298,931	97.3	240	2,573	$114,594	87	1,867	3,178	1.000*
19	125	$183,432	107	718	2,965	$127,733	124	2,150	2,736	1.000*
20	133	$201,061	98.6	744	2,568	$128,915	96.8	1,841	2,889	1.000*
21	143	$143,106	54	744	2,619	$158,739	87.1	1,893	2,094	1.000*
22	168	$155,884	125	744	2,572	$148,921	163	1,871	2,837	1.000*
23	170	$181,095	104	718	2,965	$125,989	124	2,108	2,736	1.000*
24	174	$144,353	54	718	2,965	$173,092	124	2,278	2,049	1.000*
25	180	$147,118	97.9	718	2,965	$169,082	101	2,186	2,226	1.000*
26	205	$138,227	98.6	744	2,572	$156,329	163	1,857	2,725	1.000*

Note: *A perfect ES of 1.000

example, DMU_{87}, ranked #17 among 26 DMUs by CES, shown in Table 3, is expected to be ranked #14 for the selected 18 DMUs. For comparison between [R] and E[R], the absolute rank difference (ARD) between these two ranks, ARD = |[R] – E[R]|, is computed to measure each method's rankings' robustness and is also reported in Table 4. For example, DMU_{87}, whose expected rank is #14 out of 18 DMUs, turns out to be #16, so its ARD is 2. Table 4 shows that the CES finds DMU #81 a new top-ranked one out of 18 DMUs, initially ranked #3 among 26 efficient DMUs, while the SES ranks DMU_{205} as a new top-ranked one, which is expected to be ranked #11. In addition, the columns of ARDs of CES and SES under the SSN-DEA model exhibit the DEAs' critical weakness, i.e. the inconsistency of ranking DMUs. Out of 18 DMUs, the CES and SES generate 14 DMUs and 17 DMUs with positive ARDs, respectively, with a maximum ARD of 14. In contrast, the proposed GTSN-DEA finds the same ranks for 9 DMUs, including the top-three DMUs, DMU_{174}, DMU_{180} and DMU_{143}. Table 5 reports each approach's total ARD, mean ARD and maximum ARD. The results shown in Table 5 assert that the proposed GTSN-DEA method dominates in all three measures and generates more consistent and robust rankings than the two approaches, CES and SES, of the SSN-DEA.

For further investigation, eleven (11) DMUs ranked at least #5 by any efficiency scores are selected, evaluated and reported in Table 6. The results of ARDs in Table 6 are summarized in Table 7, just like Tables 4 and 5 The CES continues to rank DMU_{81} again as a top-ranked one, while the SES, which ranks DMU_{205} No. 1 with 18 DMUs under evaluation, surprisingly identifies DMU_{87} as a No. 1 DMU. Out of these 11 DMUs, the CES approach ranks the original top 6 DMUs differently, while the SES ranks DMU_{133} and DMU_{205} so differently, with ARDs of 3 and 5, respectively. As shown in Tables 6 and 7, the proposed method's performance, which is similar to what is observed in Tables 4 and 5, shows its better consistency in ranking the DMUs than the SSN-DEA.

Tables 8–10 summarize changes in the top-five DMUs for each case generated by SSN- DEA and the transformed GTSN-DEA. As Table 10 shows, it is pretty evident that the rankings generated by GTSN-DEA do not change as significantly as the rankings generated by SSN-DEA. These results also support that the proposed GTSN-DEA method generates more robust rankings than the traditional SSN-DEA. The five top-ranked DMUs by any of the three methods are DMU_{81}, DMU_{87}, DMU_{133}, DMU_{174} and DMU_{205}, which are depicted in Figure A1, where each DMU represents the humanitarian supply chain network (HSCN) configuration, including locations and allocations of ERFs.

Both DMU_{81} by CES and DMU_{174} ranked #1 by GTSN-DEA find {Greenville, Charleston} for the CWH locations. DMU_{81} finds {Anderson, Columbia, Spartanburg} for RDCs

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Table 3 Comparison of rankings for the efficient 26 DMUs

No	DMU #	Single-Stage DEA				General Two-Stage Network DEA			
		CES	[R]	SES	[R]	θ_ω^1	θ_ω^2	θ_ω^{cen*}	[R]
1	25	0.9049	10	1.0000	25	0.5016	0.9100	0.4564	21
2	26	0.9050	9	1.0000	23	0.5016	0.9156	0.4592	20
3	28	0.8772	16	1.0145	7	0.7430	1.0000	0.7430	8
4	34	0.8988	11	1.0000	24	0.5016	0.9018	0.4523	22
5	35	0.8967	12	1.0136	8	0.5070	0.9354	0.4742	18
6	38	0.7962	23	1.0107	9	0.6525	1.0000	0.6525	13
7	39	0.8331	22	1.0000	26	0.4204	1.0000	0.4204	25
8	40	0.8338	21	1.0052	14	0.4276	1.0000	0.4276	23
9	42	0.8907	14	1.0015	21	0.6539	0.9582	0.6266	15
10	43	0.9053	8	1.0049	16	0.7591	0.9691	0.7356	11
11	81	0.9352	3	1.0216	6	0.6296	1.0000	0.6296	14
12	87	0.8550	17	1.0471	1	0.3782	1.0000	0.3782	26
13	88	0.9104	6	1.0082	12	0.5070	0.9097	0.4612	19
14	89	0.9370	2	1.0049	15	0.6934	0.8701	0.6033	16
15	91	0.8931	13	1.0291	2	0.8485	0.9799	0.8315	4
16	97	0.9131	4	1.0018	19	0.8107	0.9650	0.7823	6
17	98	0.9114	5	1.0011	22	0.7888	0.9710	0.7659	7
18	101	0.8423	20	1.0031	17	0.4240	1.0000	0.4240	24
19	125	0.8537	18	1.0016	20	0.7870	0.9382	0.7383	9
20	133	0.9400	1	1.0242	4	0.7024	0.8557	0.6010	17
21	143	0.9098	7	1.0026	18	1.0000	0.8849	0.8849	3
22	168	0.7057	25	1.0099	10	0.8867	0.8207	0.7278	12
23	170	0.8513	19	1.0094	11	0.7971	0.9254	0.7376	10
24	174	0.7654	24	1.0244	3	1.0000	0.8999	0.8999	1
25	180	0.8840	15	1.0225	5	0.9812	0.9083	0.8913	2
26	205	0.6989	26	1.0070	13	1.0000	0.8146	0.8146	5

Notes: θ_ω^1: ES at Stage 1, θ_ω^2: ES at Stage 2, θ_ω^{cen*}: Overall ES, [R]: Ranking

Table 4 Comparison of actual ranks vs. expected ranks for the top-nine DMUs by each DEA method

No	DMU #	Single-Stage DEA								General Two-Stage DEA					
		CES	[R]	E[R]	ARD	SES	[R]	E[R]	ARD	θ_ω^1	θ_ω^2	θ_ω^{cen*}	[R]	E[R]	ARD
1	26	0.8774	12	9	3	1.0034	15	18	3	0.5016	0.9624	0.4827	16	17	1
2	28	0.9078	10	13	3	1.0145	9	7	2	0.7430	1.0000	0.7430	9	8	1
3	35	0.8753	13	10	3	1.0142	10	8	2	0.5070	0.9779	0.4958	15	15	0
4	38	0.8339	15	16	1	1.0107	11	9	2	0.6525	1.0000	0.6525	11	11	0
5	43	0.9222	8	8	0	1.0057	13	13	0	0.7591	0.9727	0.7384	10	10	0
6	81	0.9385	1	3	2	1.0216	8	6	2	0.6296	1.0000	0.6296	14	12	2
7	87	0.8112	16	14	2	1.0471	3	1	2	0.3782	1.0000	0.3782	18	18	0
8	88	0.8831	11	6	5	1.0082	12	10	2	0.5070	0.9500	0.4816	17	16	1
9	89	0.9285	6	2	4	1.0049	14	12	2	0.6934	0.9131	0.6332	12	13	1
10	91	0.9260	7	11	4	1.0291	4	2	2	0.8485	0.9822	0.8334	5	4	1
11	97	0.9310	3	4	1	1.0018	17	15	2	0.8107	0.9663	0.7834	6	6	0
12	98	0.9291	5	5	0	1.0011	18	17	1	0.7888	0.9720	0.7667	7	7	0
13	125	0.8701	14	15	1	1.0492	2	16	14	0.7870	0.9624	0.7574	8	9	1
14	133	0.9310	4	1	3	1.0242	6	4	2	0.7034	0.8973	0.6312	13	14	1
15	143	0.9316	2	7	5	1.0026	16	14	2	1.0000	0.8984	0.8984	3	3	0
16	174	0.8051	17	17	0	1.0244	5	3	2	1.0000	0.9624	0.9624	1	1	0
17	180	0.9124	9	12	3	1.0225	7	5	2	0.9812	0.9293	0.9119	2	2	0
18	205	0.7141	18	18	0	1.0521	1	11	10	1.0000	0.8761	0.8761	4	5	1

Notes: ARD: Absolute Rank Difference = |[R] – E[R]|

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Table 5 Summary of rank differences for top-nine DMUs

	Single-Stage DEA		General Two-Stage DEA
	CES	SES	θ_{ω}^{cen*}
Total ARD	40	54	10
Mean ARD	2.22	3.0	0.56
Maximum ARD	5	14	2

Notes: ARD: Absolute Rank Difference = |[R] – E[R]|

covered by the CWH {Greenville} and identifies {Walterboro, Conway} for RDCs covered by the CWH {Charleston}. DMU_{174} has the edge over DMU_{81} regarding TLC (=TLC1 + TLC2), whereas DMU_{81} has a greater CDE than DMU_{174}. In terms of MCD, DMU_{174} is more efficient than DMU_{81} except for the coverage distance from RDC {Moncks Corner} to NBS {Bennettsville}. The top-ranked DMU by SES, DMU_{87}, finds two CWH locations in the middle of South Carolina, {Columbia, Florence}. As mentioned before, DMU_{87} has the highest CDE among all 26 efficient DMUs. DMU_{133}, ranked #1 by CES, finds two CWH locations, {Greenville, Columbia}, far from the coastal area and looks more balanced regarding MCD, ECD and CDE than the other three top-ranked DMUs by the SSN-DEA-based methods.

To investigate the effects of disruption risks, we perform a sensitivity analysis by changing the risk probability for the CWH location {Charleston} of DMU_{81}, which is the largest city in South Carolina and is regarded as the most susceptible to the weather among the five CWH candidate locations. If the risk probability for the location gets lower, the CWH location will not change. Thus, we gradually increase the risk probability, q_2, for {Charleston}, by 0.05 from the current probability of 0.250 and solve the WGP model with a weight set given to DMU_{81}. We check if the optimal CWH location is shifted from {Charleston} to a different location. The experiment results are summarized in Table A1, showing that the CWH location {Charleston} does not change until q_2 rises from 0.250 up to 0.295. We observe that only the performance measures related to ECD, such as ECD0, ECD1 and ECD2, decrease as long as the CWH location is not changed. When we increase q_2 from 0.295 to 0.300, the optimal CWH location is changed to {Columbia} with a higher risk probability of 0.375. Consequently, all the performance measures are also changed. Considering all five performance measures, the WGP model changes the optimal CWH location despite having a higher risk probability.

To see the effects of disruption risks more on the ERF location-allocation, we set all the probabilities of facility disruptions equal to zero, i.e. $p_j = q_i = 0, \forall j \; and \; i$. Solving the WGP model for all 286 weight sets generates only eight (8)

Table 7 Summary of rank differences for top-five DMUs

	Single-Stage DEA		General Two-Stage DEA
	CES	SES	θ_{ω}^{cen*}
Total ARD	14	14	6
Mean ARD	1.27	1.27	0.54
Maximum ARD	3	5	2

Table 8 Top five DMUs for each case by CES of SSN-DEA

Rank	Case 1: All 26 efficient DMUs under evaluation	Case 2: Top-nine DMUs under evaluation	Case 3: Top-five DMUs under evaluation
1	DMU #133	DMU #81	DMU #81
2	DMU #89	DMU #143	DMU #133
3	DMU #81	DMU #97	DMU #89
4	DMU #97	DMU #133	DMU #143
5	DMU #98	DMU #98	DMU #180

Table 9 Top five DMUs for each case by SES of SSN-DEA

Rank	Case 1: All 26 efficient DMUs under evaluation	Case 2: Top-nine DMUs under evaluation	Case 3: Top-five DMUs under evaluation
1	DMU #87	DMU #205	DMU #87
2	DMU #91	DMU #125	DMU #205
3	DMU #174	DMU #87	DMU #91
4	DMU #133	DMU #91	DMU #133
5	DMU #98	DMU #174	DMU #180

Table 10 Top five DMUs for each case by GTSN DEA

Rank	Case 1: All 26 efficient DMUs under evaluation	Case 2: Top-nine DMUs under evaluation	Case 3: Top-five DMUs under evaluation
1	DMU #174	DMU #174	DMU #174
2	DMU #180	DMU #180	DMU #180
3	DMU #143	DMU #143	DMU #143
4	DMU #91	DMU #205	DMU #205
5	DMU #205	DMU #91	DMU #91

Table 6 Comparison of actual ranks vs. expected ranks for the top-five DMUs

No	DMU #	Single-Stage DEA								General Two-Stage DEA					
		CES	[R]	E[R]	ARD	SES	[R]	E[R]	ARD	θ_{ω}^{1}	θ_{ω}^{2}	θ_{ω}^{cen*}	[R]	E[R]	ARD
1	81	0.9619	1	3	2	1.0278	6	6	0	0.6296	1.0000	0.6296	10	8	2
2	87	0.8393	9	9	0	1.1030	1	1	0	0.3782	1.0000	0.3782	11	11	0
3	89	0.9474	3	2	1	1.0096	8	8	0	0.6934	0.9188	0.6371	8	10	2
4	91	0.9192	8	7	1	1.0448	3	2	1	0.8485	1.0000	0.8485	5	4	1
5	97	0.9264	6	4	2	1.0018	11	10	1	0.8107	0.9783	0.7931	6	6	0
6	98	0.9232	7	5	2	1.0044	9	11	2	0.7888	0.9847	0.7767	7	7	0
7	133	0.9543	2	1	1	1.0242	7	4	3	0.7024	0.9030	0.6343	9	9	0
8	143	0.9372	4	6	2	1.0026	10	9	1	1.0000	0.9120	0.9120	3	3	0
9	174	0.8335	10	10	0	1.0279	4	3	1	1.0000	0.9785	0.9785	1	1	0
10	180	0.9264	5	8	3	1.0279	5	5	0	0.9812	0.9458	0.9280	2	2	0
11	205	0.7836	11	11	0	1.0739	2	7	5	1.0000	0.8854	0.8854	4	5	1

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different configurations. See Table A2. Due to zero disruption probabilities, a significant performance measure, ECD would not differ among DMUs for the single-stage process. For the two-stage network process, there are only slight differences among DMUs for ECD0 and ECD1 at stage 1 and ECD2 at stage 2. We apply CE- and SE-DEA methods for the single-stage process and the GTSN-DEA for the transformed two-stage network process. Three methods identify three different top-ranked DMUs; DMU_{87} by CE-DEA, DMU_{101} by SE-DEA and DMU_{27} by GTSN-DEA. Note that DMU_{87}, depicted in Figure A1, is selected as a top-ranked one by SE-DEA with disruption risks. From DMU_{87} in Figure A1 and the other two top-DMUs, DMU_{101} and DMU_{27}, depicting Figure A2, a significant effect of disruption risks is that all three top-rated DMUs have the common CWS location {Florence}. Note that the common CWS{Florence} has the highest disruption risk, and all three top-ranked DMUs choose the same RDCs {Rock Hill, Conway, Moncks Corner} for {Florence}.

5. Summary and conclusions

The HSCN design has been a challenging problem whose goal is to relieve and minimize the effects of disasters and pandemics. For designing more balanced HSCN schemes consisting of ERF location and allocation, a WGP model is applied to generate various HSCN configurations. To evaluate these developed supply chain network schemes to identify the most efficient ones, the single-stage network (SSN) DEA models have been applied by various authors. The traditional C-DEA evaluates DMUs in terms of self-evaluation, allowing each DMU to rate its efficiency score with the most favorable weights. Consequently, problems related to weak discriminating power have arisen as the C-DEA is applied. The reason is that multiple DMUs frequently turn out to be efficient, so the lack of discrimination power is the major weakness of the C-DEA. Several methods based on the C-DEA model have emerged to remedy this weakness and increase discrimination. The cross-efficiency (CE) evaluation methods and super-efficiency (SE) models are typical techniques for ranking DMUs. Still, many studies reveal that these DEA models frequently do not generate consistent and robust rankings.

To overcome such shortcomings of SSN-DEA, this paper proposes transforming SSN into TSN so that GTSN-DEA is applied. The case study shows that the ranks generated by the single-stage process's CE- and SE-DEA models are not as consistent or robust as the GTSN-DEA. We observe that different HSCN configurations are ranked highly by the proposed approach, and these highly ranked schemes are ranked very low by the SSN-DEA method. In addition, the rankings produced by GTSN-DEA are not affected by the network schemes to be rated, while the ranks by the SSN-DEA models depend upon them under evaluation. Thus, the contribution of the proposed approach is to reveal the could-be hidden network schemes, if SSN-DEA is only applied, that the decision-makers would not consider as the candidate schemes for their final decision. This study demonstrates that the proposed GTSN-based approach would be an essential tool for designing these kinds of supply chain network schemes.

Environmental or natural disasters are one of the most challenging disruption risks that can cause one of the most potentially damaging. Particularly as the impact of global climate change continues to flow throughout the world, ERFs are frequently entirely disrupted, as shown throughout the world these days. Complete failure is the worst case of facility disruptions, so it would be interesting to consider the effects of partial failure of ERFs on the HSCN schemes and the ranks of efficient HSCN configurations as a future research direction. This paper considers the case of facility disruptions only. Future research will significantly enhance this study if the transportation disruptions, including route and transportation mode disruptions, are integrated with this study.

Several authors suggest future research directions for better performance of various supply chain systems. Fanoodi *et al.* (2019) apply artificial neural networks (ANNs) and auto-regressive integrated moving average (ARIMA) models to predict blood platelet demands with the aim of reducing the uncertainty in the supply chain. Goli and Malmir (2020) present an integer linear model for routing relief vehicles and using the covering tour approach, where the demand of damaged areas is considered as a fuzzy member, and fuzzy credit theory is used for optimization. With the emergence of distributed ledger technology (DLT), Roeck *et al.* (2020) provide the first empirical evidence of the impact of DLT on supply chain transactions, which will enable managers to improve their assessment of DLT usage in supply chains. Baziyad *et al.* (2022) provide an overview of the internet of Things (IoT) and investigate IoT applications and challenges in the context of supply chains. They (2022) identify four fundamental stages that should be considered in deploying IoT across a supply chain to support the digitalization of future supply chains. Khiabani *et al.* (2022) present a decision support system (DSS) based on neural networks and statistical process control charts for diagnosing and controlling myocardial infarction (MI) and continuously monitoring the patient's blood pressure. Their proposed method can help physicians make better decisions in diagnosing cardiovascular diseases. All of these proposed techniques, models and methods could be implemented to enhance the performance of the humanitarian supply chain systems.

References

Aldrighetti, R., Battini, D., Ivanov, D. and Zennaro, I. (2021), "Cost of resilience and disruptions in supply chain network design models: a review and future research directions", *International Journal of Production Economics*, Vol. 235 No. 3, 108103.

Anderson, A. and Petersen, C.N. (1993), "A procedure for ranking efficient units in DEA", *Management Science*, Vol. 39 No. 1, pp. 1261-1264.

Baziyad, H., Kayvanfar, V. and Kinra, A. (2022), "Chapter 4 - The Internet of thing – an emerging paradigm to support the digitalization of future supply chains", in MacCarthy, B.L. and Ivanov, D. (Eds), *The Digital Supply Chain*, Elsevier, pp. 61-76.

Boonmee, C., Arimura, M. and Asada, T. (2017), "Facility location optimization model for emergency humanitarian

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logistics", *International Journal of Disaster Risk Reduction*, Vol. 24, pp. 485-498.

Cao, C., Li, C., Yang, Q., Liu, Y. and Qu, T. (2018), "A novel multi-objective programming model of relief distribution for sustainable disaster supply chain in large-scale natural disasters", *Journal of Cleaner Production*, Vol. 174, pp. 1422-1435.

Charnes, A., Cooper, W.W. and Rhodes, E. (1978), "Measuring the efficiency of decision-making units", *European Journal of Operational Research*, Vol. 2 No. 6, pp. 429-444.

Charnes, A., Haag, S., Jaska, P. and Semple, J. (1992), "Sensitivity of efficiency classifications in the additive model of data envelopment analysis", *International Journal of Systems Science*, Vol. 23 No. 5, pp. 789-798.

Cook, W.D. and Zhu, J. (2014), "DEA for two-stage networks: efficiency decompositions and modeling techniques", in Cook, W.D. and Zhu, J. (Eds), *Data Envelop Analysis: A Handbook on the Modeling of Internal Structures and Networks*, Springer, NY, pp. 1-29.

Doyle, J. and Green, R. (1994), "Efficiency and cross-efficiency in DEA: derivations, meanings and uses", *Journal of Operational Research Society*, Vol. 45 No. 5, pp. 567-578.

Fanoodi, B., Malmir, B. and Jahantigh, F.F. (2019), "Reducing demand uncertainty in the platelet supply chain through artificial neural networks and ARIMA models", *Computers in Biology and Medicine*, Vol. 113, 103415.

Ganesh, A.D. and Kalpana, P. (2022), "Future of artificial intelligence and its influence on supply chain risk management – A systematic review", *Computers and Industrial Engineering*, Vol. 169, 108206.

Goli, A. and Malmir, B. (2020), "A covering tour approach for disaster relief locating and routing with fuzzy demand", *International Journal of Intelligent Transportation Systems Research*, Vol. 18, pp. 140-152.

Gress, E.S.H., Hernandez-Gress, N. and Contla, K.S. (2021), "Methodology for designing humanitarian supply chains: distribution of COVID-19 vaccines in Mexico", *Administrative Sciences*, Vol. 11 No. 4, p. 134.

Habib, M.S., Lee, Y.H. and Memon, M.S. (2016), "Mathematical models in humanitarian supply chain management: a systematic literature review", *Mathematical Problems in Engineering*, Vol. 2016, 3212095.

Hong, J.D. and Jeong, K.Y. (2019), "Humanitarian supply chain network design using data envelopment analysis and multi-objective programming models", *European Journal of Industrial Engineering*, Vol. 13 No. 5, pp. 651-680.

Khiabani, S.J., Batani, A. and Khanmohammadi, E. (2022), "A hybrid decision support system for heart failure diagnosis using neural networks and statistical process control", *Healthcare Analytics*, Vol. 2, 100110.

Li, Y., Chen, Y., Liang, L. and Xie, J. (2012), "DEA models for extended two-stage network structures", *Omega*, Vol. 40, pp. 611-618.

Li, Y., Zobel, C.W., Seref, O. and Chatfield, D. (2020), "Network characteristics and supply chain resilience under conditions of risk propagation", *International Journal of Production Economics*, Vol. 223, 107529.

Liu, C., Kou, G., Peng, Y. and Alsaadi, F.E. (2019), "Location-routing problem for relief distribution in the early post-earthquake stage from the perspective of fairness", *Sustainability*, Vol. 11 No. 3420, pp. 1-16.

Malmir, B. and Zobel, C.W. (2021), "An applied approach to multi-criteria humanitarian supply chain planning for pandemic response", *Journal of Humanitarian Logistics and Supply Chain Management*, Vol. 11 No. 2, pp. 320-346.

Monfared, M.A.S. and Safi, M. (2013), "Network DEA: an application to analysis of academic performance", *Journal of Industrial Engineering International*, Vol. 9 No. 15, pp. 1-10.

Petrudi, S.H.H., Tavana, M. and Abdi, M. (2020), "A comprehensive framework for analyzing challenges in humanitarian supply chain management: a case study of the Iranian Red Crescent Society", *International Journal of Disaster Risk Reduction*, Vol. 42, 101340, p. 20.

Ragsdale, C.T. (2018), *Spreadsheet Modeling and Decision Analysis: A Practical Introduction to Business Analytics*, 8th ed., Cengage Learning, MA.

Roeck, D., Sternberg, H. and Hofmann, E. (2020), "Distributed ledger technology in supply chains: a transaction cost perspective", *International Journal of Production Research*, Vol. 58 No. 7, pp. 2124-2141.

Sarma, D., Das, A. and Bera, U.K. (2020), "Uncertain demand estimation with optimization of time and cost using Facebook disaster map in emergency relief operation", *Applied Soft Computing*, Vol. 87, 105992.

Sexton, T.R., Silkman, R.H. and Hogan, A.J. (1986), "Data envelopment analysis: critique and extensions", in Silkman, R. (Ed.), *Measuring Efficiency: An Assessment of Data Envelopment Analysis*, Jossey-Bass, pp. 73-105.

Snyder, L.V., Atan, Z., Peng, P., Rong, Y., Schmitt, A.J. and Sinsoysal, B. (2016), "OR/MS model for supply chain disruptions: a review", *IIE Transactions*, Vol. 48 No. 2, pp. 89-109.

Van Wassenhove, L.N. (2006), "Blackett memorial lecture. Humanitarian aid logistics: supply chain management in high gear", *Journal of the Operational Research Society*, Vol. 57 No. 5, pp. 475-489.

Zhang, J., Wang, Z. and Ren, F. (2019), "Optimization of humanitarian relief supply chain reliability: a case study of the Ya'an earthquake", *Annals of Operations Research*, Vol. 283, pp. 1551-1572.

Zhu, J. (2022), "DEA under big data: data-enabled analytics and network data envelopment analysis", *Annals of Operations Research*, Vol. 309 No. 2, pp. 761-783.

Further reading

Abdul Rahman, N.A., Ahmi, A., Jraisat, L. and Upadhyay, A. (2022), "Examining the trend of humanitarian supply chain studies: pre, during and post COVID-19 pandemic", *Journal of Humanitarian Logistics and Supply Chain Management*, Vol. 12 No. 24, pp. 594-617, doi: 10.1108/JHLSCM-01-2022-0012.

Liu, K., Zhang, H. and Zhang, Z.H. (2021), "The efficiency, equity and effectiveness of location strategies in humanitarian logistics: a robust chance-constrained approach", *Transportation Research Part E: Logistics and Transportation Review*, Vol. 156 No. 2021, 102521.

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Nahr, J.G. and Bathaee, M. (2021), "Design of a humanitarian logistics network considering the purchase contract", *Journal of Decisions and Operations Research*, Vol. 6 No. 3, pp. 423-444.

Xu, W., Xiong, S., Proverbs, D. and Zhong, Z. (2021), "Evaluation of humanitarian supply chain resilience in flood disaster", *Water*, Vol. 13 No. 16, pp. 1-21, 2158.

Appendix. List of some acronyms

ARD	Absolute Rank Difference
CDE	Covered Demand in case of Emergency
CDP	Commodity Distribution Point
CE	Cross Efficiency
CES	Cross Efficiency Score
CWH	Central Warehouse
DEA	Data Envelopment Analysis
C-DEA	Conventional DEA
CE-DEA	Cross Efficiency DEA
GTSN-DEA	General Two-Stage Network DEA
SE-DEA	Super Efficiency DEA
SSN-DEA	Single-Stage Network DEA
DMU	Decision-Making Unit
ES	Efficient Score
ECD	Expected Amount of Covered Demand
ERF	Emergency Response Facility
HSCN	Humanitarian Supply Chain Network
GP	Goal Programming
MCD	Maximum Coverage Distance
NBS	Neighborhood Site
RDC	Relief Distribution Center
SCRM	Supply Chain Risk Management
SES	Super Efficiency Score
TLC	Total Logistics Cost
WGP	Weighted Goal Programming

Table A1 The effect of disruption risks on the CWH location of DMU_{81}

Risk probability (q_2)	CWH location	TLC1 Input (1,1)	MCD1 Input (1, 2)	ECD0 (K) Output (1,1)	ECD1 (K) Output (1,2)	TLC2 Input (2, 1)	MCD2 Input (2, 2)	ECD2 (K) Output (2,1)	CDE (K) Output (2,2)
0.250	{Charleston}	$229,285	104	718	2,965	$102,438	82.9	2,093	2,827
...	{Charleston}	...	...	...	...	...	...	...	...
0.295	{Charleston}	$229,285	104	702	2,890	$102,438	82.9	2,040	2,827
0.300	{Columbia}	$204,336	99	744	2,614	$138,925	97	1,902	2,889

Table A2 Efficient DMUs, their performance metrics and efficiency scores for the case of no disruption risks

No	DMU #	TLC1 Input (1,1)	MCD1 Input (1, 2)	ECD0 (K) Output (1,1)	ECD1 (K) Output (1,2)	TLC2 Input (2, 1)	MCD2 Input (2, 2)	ECD2 (K) Output (2,1)	CDE (K) Output (2,2)	ES
1	27	$322,684	97.3	387	4,109	$109,153	87	4,109	3,178	1.000*
2	33	$306,960	97.3	387	4,109	$138,467	93	4,109	3,178	1.000*
3	34	$310,665	97.3	387	4,109	$121,956	95.7	4,109	3,178	1.000*
4	39	$312,731	97.3	387	4,109	$119,623	92	4,109	3,178	1.000*
5	40	$311,411	97.3	387	4,109	$130,072	93	4,109	3,178	1.000*
6	81	$279,656	104	664	3,832	$105,574	92	3,832	3,361	1.000*
7	101	$298,931	97.3	387	4,109	$114,594	87	4,109	3,178	1.000*
8	127	$155,884	125	982	3,514	$148,921	163	3,514	2,837	1.000*

Note: *A perfect ES of 1.000

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Figure A1 The five most efficient HSCN network schemes

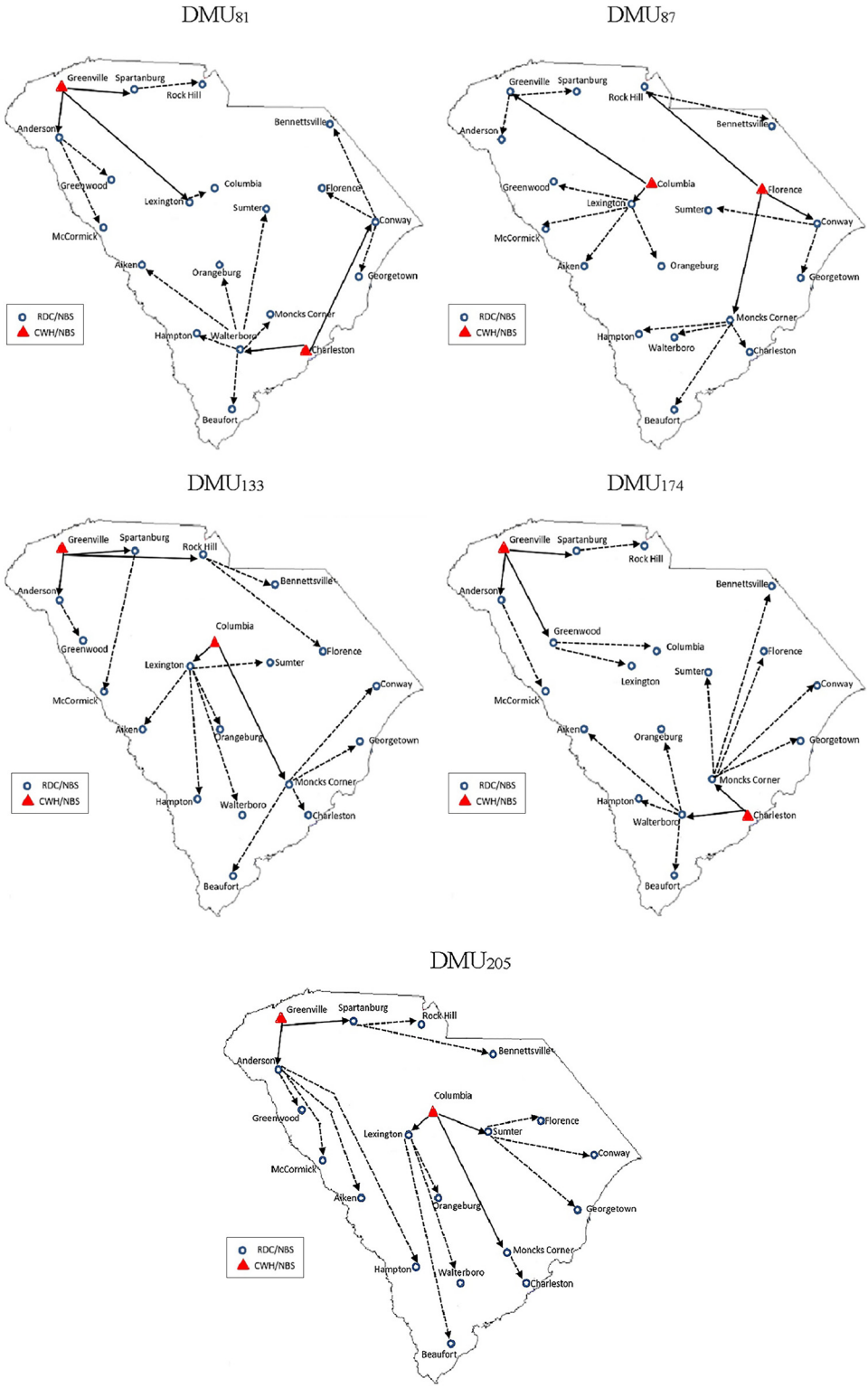

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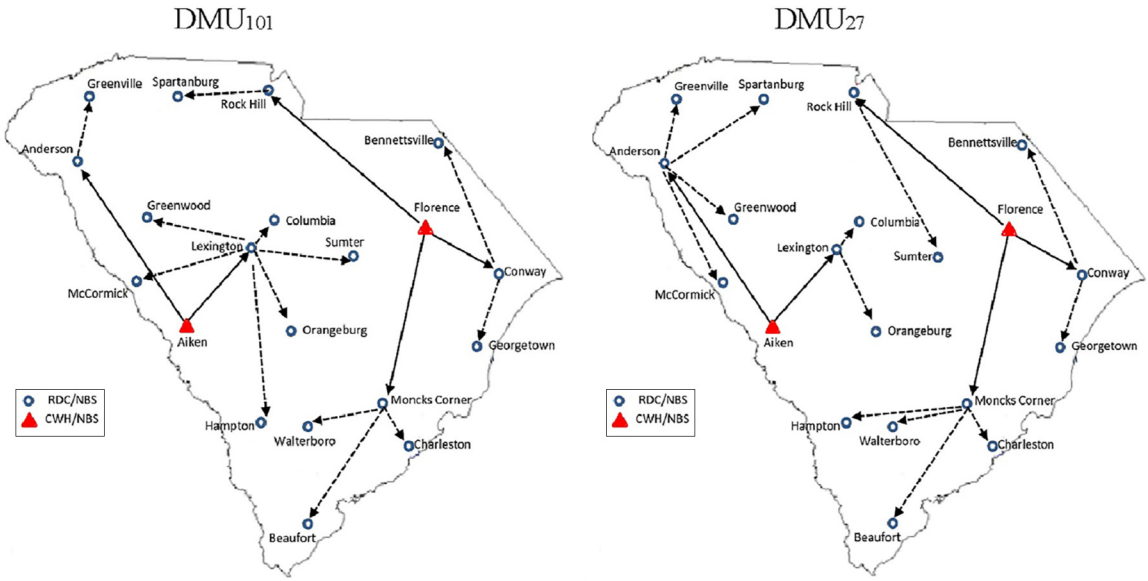
Figure A2 The most efficient HSCN network schemes for the case of no disruption risks



Notes: For DMU_{87}, See Figure A1

About the author

Dr Jae-Dong Hong is a distinguished professor in industrial engineering at South Carolina State University. He holds a BS degree from Korea University and his MS and PhD from the Pennsylvania State University, all in industrial engineering. His research interests are modeling various logistics network systems and designing efficient supply chain systems. He has published more than 110 papers in various international journals and proceedings. He is a two-time winner of the Best Paper Award, including the *Best Overall Conference Paper Award* at the 2021 NEDSI Conference. He received the *South Carolina Governor's Distinguished Professor Award*, among many prestigious awards. Jae-Dong Hong can be contacted at: jhong@scsu.edu

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